

# 基于Fredholm多核学习的半监督知识迁移

## Fredholm Multiple Kernel Learning for Semi-Supervised Domain Adaptation

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### Motivation

#### Semi-Supervised Domain Adaptation:

- Use **labeled source** and **target data**: adapting traditional models (e.g., SVM, logistic regression) to the target domain;
- Use **unlabeled target data**: coping with the inconsistency of two data distributions.

#### Challenges:

- Ignore **unlabeled target data** in the process of learning adaptive classifiers, while the unlabeled data is desirable for **robustness** and **noise resiliency**.

#### Semi-Supervised Kernel Prediction:

- Based on Fredholm integral, use **labeled** and **unlabeled data** samples for noise suppression.

Learn a predictive function over the RKHS  $\mathcal{H}$ :  
where  $f = \arg \min_{f \in \mathcal{H}} \frac{1}{n} \sum_{i=1}^n L(K_P f(\mathbf{x}_i), y_i) + \beta \|f\|_{\mathcal{H}}^2$   
is the Fredholm integral  
 $K_P$

and  $K_P f(\mathbf{x}) = \int k^P(\mathbf{x}, \mathbf{z}) f(\mathbf{z}) P(\mathbf{z}) d\mathbf{z}$   
is a predefined outside kernel.  
 $k^P(\mathbf{x}, \mathbf{z})$

#### Challenges:

- Effective only when labeled and unlabeled data has **the same distribution**.
- Rely on **the single** and the choice heavily influences the performance.  
 $k^P(\mathbf{x}, \mathbf{z})$

### Contributions

- A novel domain adaptation method: **Transfer Fredholm Multiple Kernel Learning**.
- A predictive model for **noise resiliency**, **facilitating knowledge transfer** and **analyzing diverse data characteristics**.
- A simple but efficient procedure, guaranteeing rapid **convergence**.

### Transfer Fredholm Multiple Kernel Learning

$$[f, \mathbf{K}] = \arg \min_{f, \mathbf{K}} \ell(f, \mathbf{K}, D_s, D_t) + \theta \Omega(d_{\mathbf{K}}(D_s, D_t)),$$

Adapting Kernel Prediction
Reducing Distribution Mismatch

#### Adapting Kernel Prediction:

- Construct two Fredholm integrals on the two domains respectively:

$$\ell(f, \mathbf{K}, D_s, D_t) = \arg \min_{f \in \mathcal{H}} \{\beta \|f\|_{\mathcal{H}}^2 + \frac{\lambda_s}{n_s} \sum_{i=1}^{n_s} L(K_{P_s} f(\mathbf{x}_i^s), y_i^s) + \frac{\lambda_t}{n_t} \sum_{i=1}^{n_t} L(K_{P_t} f(\mathbf{x}_i^t), y_i^t)\},$$

#### Reducing Mismatch of Distributions:

- Consider the learnt kernel  $\mathbf{K}$  as a convex combination of given (base) kernels:

$$\mathbf{K}(\mathbf{x}_i, \mathbf{x}_j) = \sum_{m=1}^M d_m \mathbf{K}_m(\mathbf{x}_i, \mathbf{x}_j)$$

- Maximum Mean Discrepancy (MMD):

$$d_{\mathbf{K}}(D_s, D_t) = \left\| \frac{1}{n_s} \sum_{i=1}^{n_s} \phi(\mathbf{x}_i^s) - \frac{1}{n_u + n_t} \sum_{i=1}^{n_u + n_t} \phi(\mathbf{x}_i^t) \right\|_{\mathcal{H}}^2 = \text{tr}(\Phi^T \Phi \mathbf{S}) = \text{tr}(\mathbf{K} \mathbf{S}),$$

- Reducing mismatch is translated to the choice of optimal weights  $d_m$ :

$$\Omega(d_{\mathbf{K}}(D_s, D_t)) = (\text{tr}((\sum_{m=1}^M d_m \mathbf{K}_m) \mathbf{S}))^2 = \mathbf{d}^T \mathbf{p} \mathbf{p}^T \mathbf{d},$$

#### Implementation:

- Cost function:

$$\min_{\mathbf{d}} J(\mathbf{d}) \quad \text{with } d_m \geq 0, \sum_{m=1}^M d_m = 1,$$

where  $J(\mathbf{d}) = \min_{f \in \mathcal{H}} \{\beta \|f\|_{\mathcal{H}}^2 + \frac{\lambda_s}{n_s} \sum_{i=1}^{n_s} (K_{P_s} f(\mathbf{x}_i^s) - y_i^s)^2 + \frac{\lambda_t}{n_t} \sum_{i=1}^{n_t} (K_{P_t} f(\mathbf{x}_i^t) - y_i^t)^2 + \theta \mathbf{d}^T \mathbf{p} \mathbf{p}^T \mathbf{d}\}.$

### Experiments

#### Synthetic Example

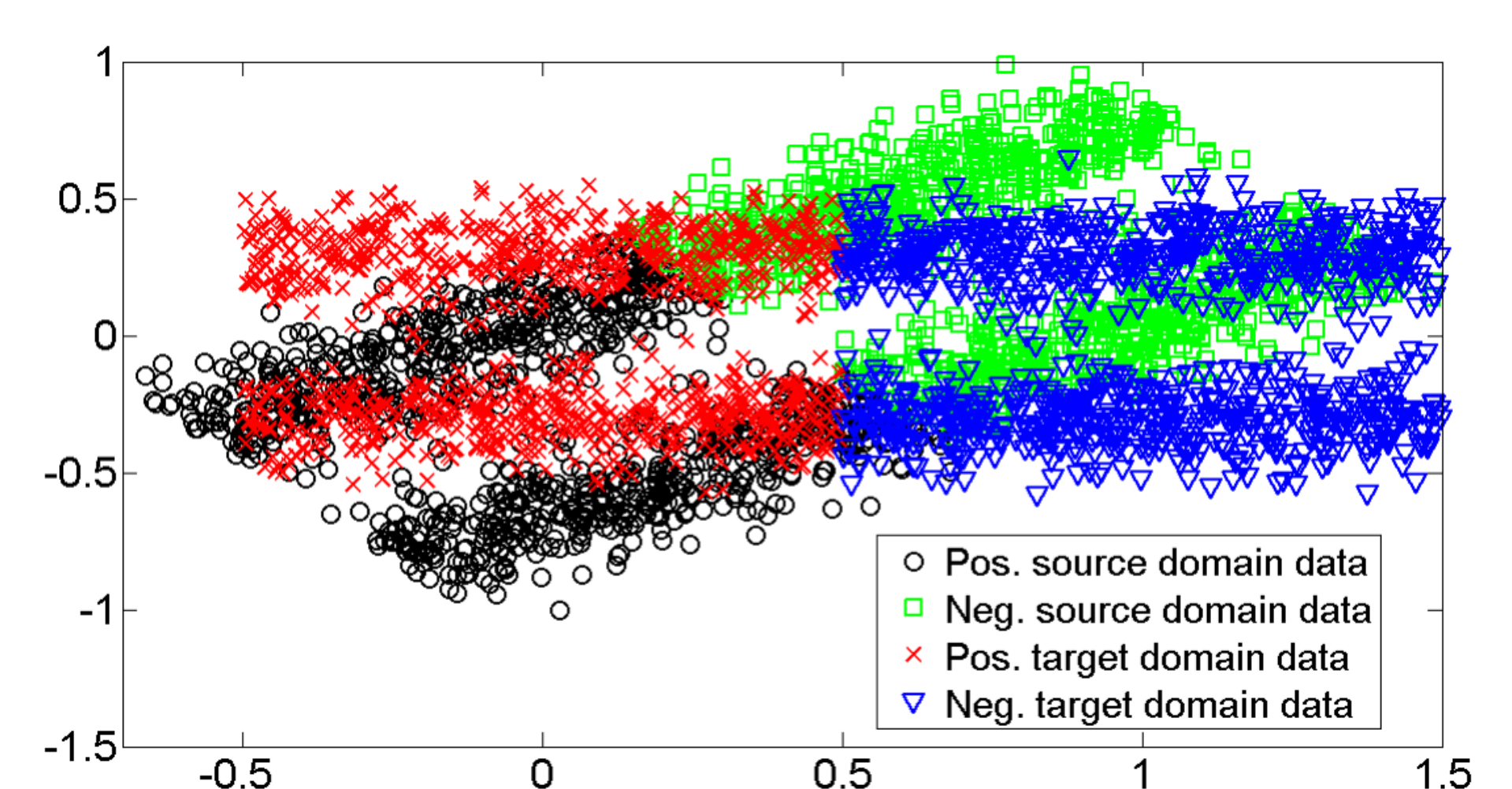


Table 1: Classification accuracy and standard error.

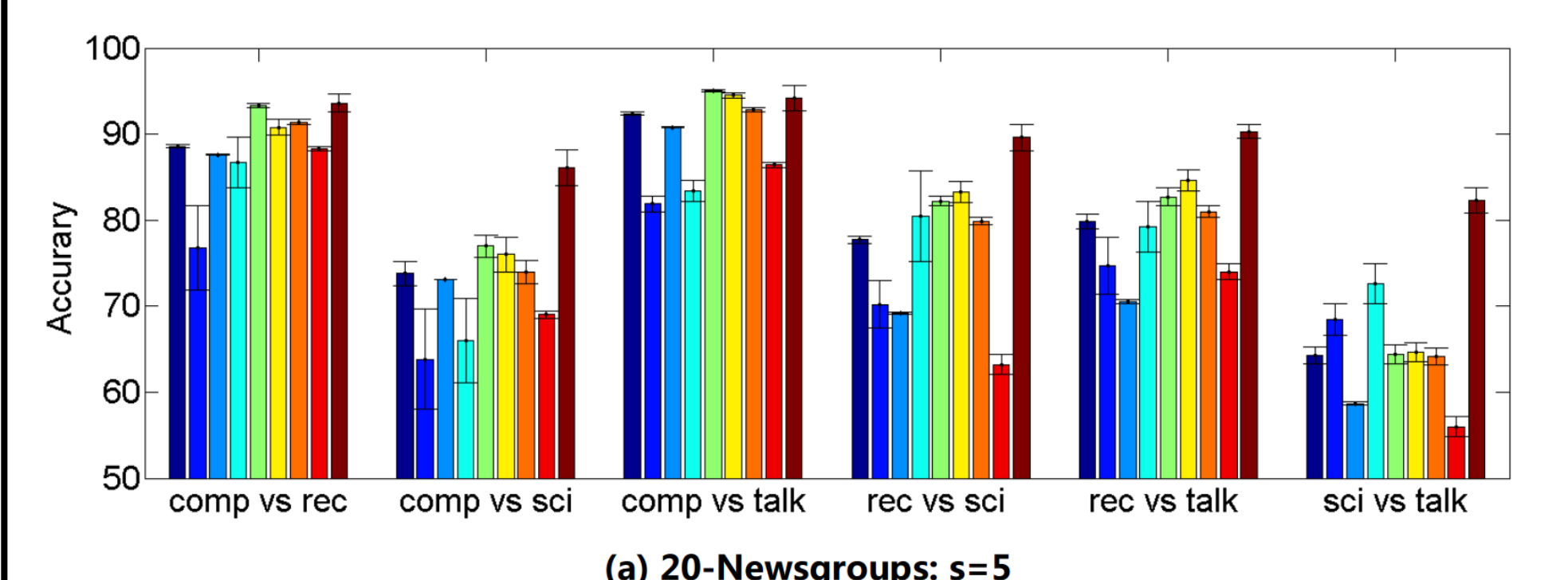
SVM-st	Fred-st	DTMKL-f	TFMKL
87.86±0.02	90.95±0.01	91.07±0.01	96.02 ±0.11

#### Object Recognition

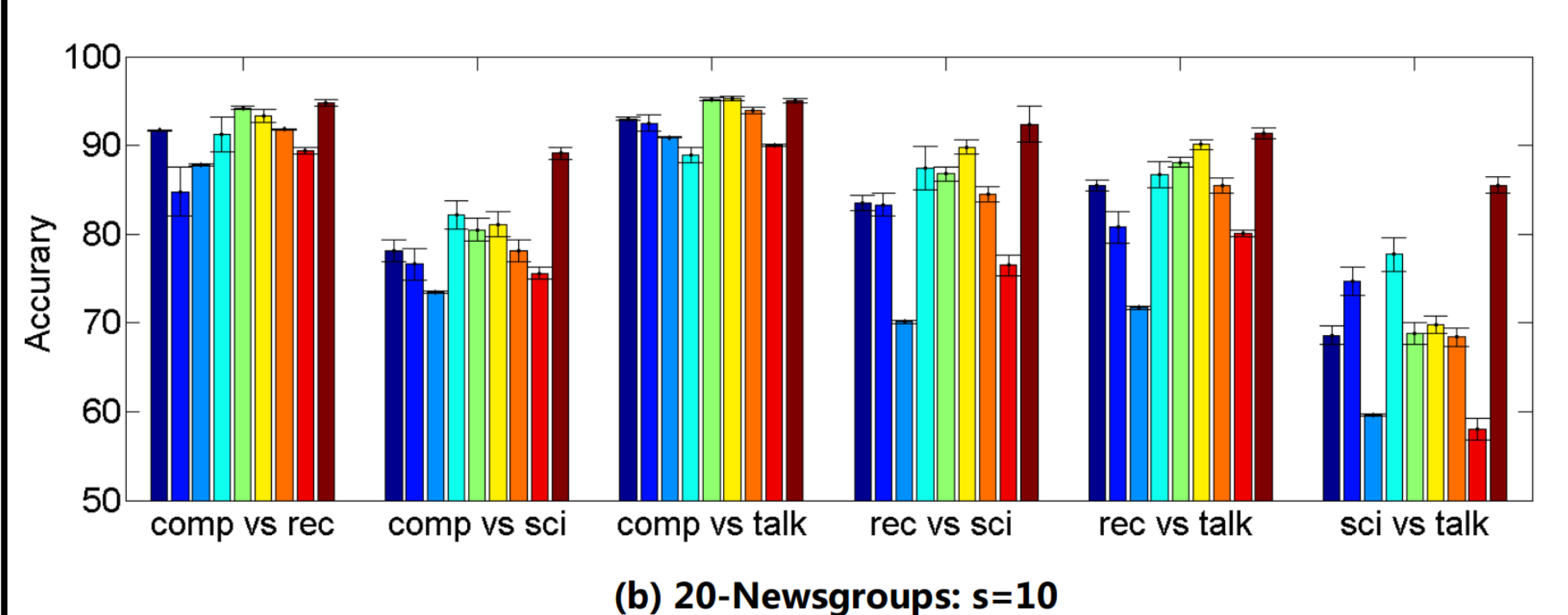
Table 2: Classification accuracy and standard error on the 12 cross-domain object categorization data sets. The best recognition rates are in red and bold font. The second best recognition rates are in blue and italic font.

Data Set	SVM-st	SVM-t	Fred-st	Fred-t	DTMKL-f	MMDT	KMM	GFK	TFMKL
A→D	45.6±0.7	55.9±0.8	46.4±0.8	<b>58.2±0.9</b>	46.4±0.7	56.7±1.3	49.0±0.7	50.7±0.8	<b>62.1±0.9</b>
A→W	46.3±0.7	62.4±0.9	50.3±0.9	<i>69.2±1.1</i>	48.8±0.8	64.6±1.2	47.4±0.9	58.6±1.0	<b>69.8±0.9</b>
A→C	39.8±0.3	32.0±0.8	39.0±0.4	35.3±0.9	40.5±0.4	36.4±0.8	<b>40.8±0.3</b>	36.0±0.5	<b>43.6±0.6</b>
D→A	41.6±0.4	45.7±0.9	51.5±0.5	<i>51.7±0.8</i>	42.6±0.4	46.9±1.0	42.6±0.4	45.7±0.6	<b>52.9±0.7</b>
D→W	77.4±0.6	62.1±0.8	<b>82.4±0.3</b>	65.4±0.8	76.1±0.5	74.1±0.8	<i>78.5±0.6</i>	76.5±0.5	77.8±0.6
D→C	35.9±0.4	31.7±0.6	<i>37.7±0.4</i>	35.2±0.8	37.5±0.5	34.1±0.8	36.9±0.4	32.9±0.5	<b>37.9±0.4</b>
W→A	43.4±0.3	45.6±0.7	49.5±0.5	<i>52.7±0.7</i>	45.5±0.4	47.7±0.9	44.4±0.5	44.1±0.4	<b>54.4±0.4</b>
W→D	69.5±0.8	55.1±0.8	<b>73.2±0.6</b>	58.2±0.8	69.9±1.1	67.0±1.1	70.4±0.8	<i>70.5±0.7</i>	67.7±0.9
W→C	36.4±0.4	30.4±0.7	37.5±0.3	34.6±0.9	<b>37.8±0.4</b>	32.2±0.8	<i>37.6±0.4</i>	31.1±0.6	36.1±0.8
C→A	46.9±0.6	45.3±0.9	<i>52.7±0.6</i>	49.9±1.0	49.5±0.9	49.4±0.8	48.0±0.6	44.7±0.8	<b>54.2±0.9</b>
C→D	52.0±1.0	55.8±0.9	55.7±0.9	59.2±1.1	53.1±0.9	56.5±0.9	53.0±1.0	<i>57.7±1.1</i>	<b>59.2±1.1</b>
C→W	55.6±0.9	60.3±1.0	60.6±1.2	62.0±1.1	55.4±1.1	<b>61.8±1.1</b>	54.6±0.9	63.7±0.8	<b>68.2±0.9</b>
Mean	49.0±0.6	48.5±0.8	<b>52.9±0.6</b>	52.3±0.8	50.2±0.7	52.5±1.0	50.3±0.6	51.0±0.7	<b>57.0±0.8</b>

#### Text Classification



(a) 20-NewsGroups: s=5



(b) 20-NewsGroups: s=10