An Addendum to the ZUC-256 Stream Cipher

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Abstract. ZUC-256 is a stream cipher, together with AES-256 and SNOW-V, proposed as the core primitive in future set of 3GPP confidentiality and integrity algorithms for the upcoming 5G applications which offer the 256-bit security.

While the original initialization scheme of ZUC-256 can work with a 256-bit key and an IV of length up to 184 bits, we describe a new initialization scheme of ZUC-256 that supports an IV of the exact 128 bits in this paper. Compared to the original initialization scheme, this new key/IV setup algorithm avoids the division of the whole key/IV byte and provides a simple and natural-looking initialization scheme for ZUC-256.

Keywords: 5G, Stream ciphers, ZUC, 256-bit security.

1 Introduction

The core of the 3GPP confidentiality and integrity algorithms 128-EEA3 and 128-EIA3 is the ZUC-128 stream cipher [1]. ZUC-256 is a new member in the ZUC family of stream ciphers, formally proposed in 2018 for the intended usage in the upcoming 5G applications for 3GPP. ZUC-256 stream cipher is industrial-friendly, differing from ZUC-128 only in the initialization phase and in the message authentication codes (MAC) generation phase. It works with a 256-bit key and a 184-bit initialization vector (IV) and generates a keystream frame of length from 20000 to 2^{32} bits after each mixture of the original data.

After the publication of ZUC-256, there is an increasing interest of evaluating its security against various cryptanalytic approaches. At the ZUC-256 international conference in 2018 [6], there are several talks that analyzed different aspects of its security, all of which imply that ZUC-256 is secure against the corresponding cryptanalysis method. Then, a linear distinguishing attack is presented in [5] at FSE 2020, requiring a exceptionally-long keystream frame, which is out of the security claim in [7], as analyzed in [4]. For the initialization phase, there is a differential analysis published in [3].

In this paper, we propose a new initialization scheme of ZUC-256 that works with a 256-bit key and a 128-bit IV. This new key/IV setup scheme avoids the division of the whole key/IV byte, is simple and natural-looking, and also provides the 256-bit security in 5G applications. A brief cryptanalysis of the new initialization scheme is also yielded.

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This paper is structured as follows. In Section 2, we give the detailed description of ZUC-256 with the new initialization scheme, including the initialization phase, the keystream generation phase and the MAC generation phase for completeness. The cryptanalysis related to the change of the IV size and the key/IV loading scheme will be discussed in Section 3. Finally, some conclusions are drawn in Section 4.

$\mathbf{2}$ The Description



Fig. 1. The initialization phase of the ZUC-256 stream cipher

In this section, we will present the detailed description of the new initialization scheme of ZUC-256 stream cipher. The following notations will be used hereafter.

- Denote the integer modular addition by $\boxplus,$ i.e., for $0 \leq x < 2^{32}$ and $0 \leq y <$
- 2³², $x \boxplus y$ is the integer addition modulo 2^{32} . Denote the integer addition modulo $2^{31} 1$ by $x + y \mod (2^{31} 1)$ for $1 \le x \le 2^{31} 1$ and $1 \le y \le 2^{31} 1$.
- Denote the bitwise exclusive OR by \oplus .
- Denote the bit string concatenation by \parallel .
- $K = (K_{31}, K_{30}, ..., K_2, K_1, K_0)$, the 256-bit secret key used in the ZUC-256 where K_i for $0 \le i \le 31$ are 8-bit bytes.

- $IV = (IV_{15}, \ldots, IV_1, IV_0)$, the 128-bit initialization vector used in the ZUC-256 where IV_i for $0 \le i \le 15$ are 8-bit bytes.
- d_i for $0 \le i \le 15$ are the 7-bit constants used in the ZUC-256 stream cipher.
- \ll , the left rotation of a 64-bit operand, $x \ll n$ means $((x \ll n) \mid (x \gg$ (64 - n))).

As depicted in Fig.1, there are 3 parts involved in ZUC-256: a 496-bit linear feedback shift register (LFSR) defined over the field $GF(2^{31} - 1)$, consisting of 16 31-bit cells $(s_{15}, s_{14}, \dots, s_2, s_1, s_0)$ defined over the set $\{1, 2, \dots, 2^{31} - 1\}$; a bit reorganization layer (BR), which extracts the content of the LFSR to form 4 32-bit words, (X_0, X_1, X_2, X_3) , used in the following finite state machine (FSM); there are 2 32-bit words R_1 and R_2 used as the memory in the FSM.

The Key/IV loading scheme is as follows.

$$\begin{split} s_0 &= K_0 \parallel d_0 \parallel K_{16} \parallel K_{24} \\ s_1 &= K_1 \parallel d_1 \parallel K_{17} \parallel K_{25} \\ s_2 &= K_2 \parallel d_2 \parallel K_{18} \parallel K_{26} \\ s_3 &= K_3 \parallel d_3 \parallel K_{19} \parallel K_{27} \\ s_4 &= K_4 \parallel d_4 \parallel K_{20} \parallel K_{28} \\ s_5 &= K_5 \parallel d_5 \parallel K_{21} \parallel K_{29} \\ s_6 &= K_6 \parallel d_6 \parallel K_{22} \parallel K_{30} \\ s_7 &= K_7 \parallel d_7 \parallel IV_0 \parallel IV_8 \\ s_8 &= K_8 \parallel d_8 \parallel IV_1 \parallel IV_9 \\ s_9 &= K_9 \parallel d_9 \parallel IV_2 \parallel IV_{10} \\ s_{10} &= K_{10} \parallel d_{10} \parallel IV_3 \parallel IV_{11} \\ s_{11} &= K_{11} \parallel d_{11} \parallel IV_4 \parallel IV_{12} \\ s_{12} &= K_{12} \parallel d_{12} \parallel IV_5 \parallel IV_{13} \\ s_{13} &= K_{13} \parallel d_{13} \parallel IV_6 \parallel IV_{14} \\ s_{14} &= K_{14} \parallel d_{14} \parallel IV_7 \parallel IV_{15} \\ s_{15} &= K_{15} \parallel d_{15} \parallel K_{23} \parallel K_{31} \end{split}$$

where the constants d_i for $0 \le i \le 15$ are defined as follows, which is based on the binary expansion of π including the integer part.

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$$d_0 = 1100100$$

 $d_1 = 1000011$
 $d_2 = 1111011$

 $d_3 = 0101010$ $d_4 = 0010001$ $d_5 = 0000101$ $d_6 = 1010001$ $d_7 = 1000010$ $d_8 = 0011010$ $d_9 = 0110001$ $d_{10} = 0011000$ $d_{11} = 1100110$ $d_{12} = 0010100$ $d_{13} = 0101110$ $d_{14} = 0000001$ $d_{15} = 1011100.$

Note that there is no hidden weakness introduced in the above constants. There are 32 + 1 = 33 rounds of initialization in the ZUC-256, which is depicted as follows.

- 1. Load the key, IV and constants into the LFSR as specified above.
- 2. Let $R_1 = R_2 = 0$.
- 3. for i = 0 to 31 do
 - Bitreorganization()
 - $Z = F(X_0, X_1, X_2)$
 - LFSRWithInitializationMode($Z \gg 1$)
- 4. Bitreorganization()
 - $Z = F(X_0, X_1, X_2)$ and discard Z
 - LFSRWithworkMode().

Now we specify the relevant subroutines one-by-one.

LFSRWithInitializationMode(u)

- 1. $v = 2^{15} \cdot s_{15} + 2^{17} \cdot s_{13} + 2^{21} \cdot s_{10} + 2^{20} \cdot s_4 + (1+2^8) \cdot s_0 \mod(2^{31}-1)$ 2. if v = 0 then set $v = 2^{31} 1$
- 3. $s_{16} = v + u \mod(2^{31} 1)$
- 4. if $s_{16} = 0$ then set $s_{16} = 2^{31} 1$
- 5. $(s_{16}, s_{15}, \cdots, s_2, s_1) \to (s_{15}, s_{14}, \cdots, s_1, s_0).$

LFSRWithworkMode()

- 1. $s_{16} = 2^{15} \cdot s_{15} + 2^{17} \cdot s_{13} + 2^{21} \cdot s_{10} + 2^{20} \cdot s_4 + (1+2^8) \cdot s_0 \mod(2^{31}-1)$ 2. if $s_{16} = 0$ then set $s_{16} = 2^{31} 1$
- 3. $(s_{16}, s_{15}, \cdots, s_2, s_1) \to (s_{15}, s_{14}, \cdots, s_1, s_0).$

Bitreorganization()

1. $X_0 = s_{15H} \parallel s_{14L}$ 2. $X_1 = s_{11L} \parallel s_{9H}$ 3. $X_2 = s_{7L} \parallel s_{5H}$ 4. $X_3 = s_{2L} \parallel s_{0H}$,

where s_{iH} is the high 16 bits of the cell s_i and s_{jL} is the low 16 bits of the cell s_j .

 $F(X_0, X_1, X_2)$

- 1. $W = (X_0 \oplus R_1) \boxplus R_2$
- 2. $W_1 = R_1 \boxplus X_1$
- 3. $W_2 = R_2 \oplus X_2$
- 4. $R_1 = S(L_1(W_{1L} \parallel W_{2H}))$
- 5. $R_2 = S(L_2(W_{2L} \parallel W_{1H})),$

where $S = (S_0, S_1, S_0, S_1)$ is the 4 parallel S-boxes which are the same as those used in the previous ZUC-128 and L_1 and L_2 are the two MDS matrices used in the ZUC-128. The ZUC-256 stream cipher generates a 32-bit keystream word at each time instant.

KeystreamGeneration()

- 1. Bitreorganization()
- 2. $Z = F(X_0, X_1, X_2) \oplus X_3$
- 3. LFSRWithworkMode().

ZUC-256 generates from 20000-bit up to 2^{32} -bit keystream for each frame; after that a key/IV re-synchronization is performed with the key/constants fixed and the IV changing into a new value.

The MAC generation algorithm of ZUC-256 is as follows. Let $M = (m_0, m_1, \dots, m_{l-1})$ be the *l*-bit length plaintext message and the size *t* of the tag is selectively to be of 32, 64 and 128 bits.

 $MAC_Generation(M)$

- 1. Let ZUC-256 produce a keystream of $L = \lceil \frac{l}{32} \rceil + 2 \cdot \frac{t}{32}$ words. Denote the keystream bit string by $z_0, z_1, \dots, z_{32 \cdot L-1}$, where z_0 is the most significant bit of the first output keystream word and z_{31} is the least significant bit of the first keystream word.
- 2. Initialize $Tag = (z_0, z_1, \cdots, z_{t-1})$
- 3. for i = 0 to l 1 do
 - let $W_i = (z_{t+i}, \cdots, z_{i+2t-1})$
 - if $m_i = 1$ then $Tag = Tag \oplus W_i$
- 4. $W_l = (z_{l+t}, \cdots, z_{l+2t-1})$
- 5. $Tag = Tag \oplus W_l$
- 6. return Tag

For the different sizes of the MAC tag, to prevent the forgery attack, the constants are specified as follows.

1. for the tag size of 32 bits, the constants are

$$\begin{array}{l} d_0 = 1100100 \\ d_1 = 1000011 \\ d_2 = 1111010 \\ d_3 = 0101010 \\ d_4 = 0010001 \\ d_5 = 0000101 \\ d_6 = 1010001 \\ d_7 = 1000010 \\ d_8 = 0011010 \\ d_9 = 0110001 \\ d_{10} = 0011000 \\ d_{11} = 1100110 \\ d_{12} = 0010100 \\ d_{13} = 0101110 \\ d_{14} = 0000001 \\ d_{15} = 1011100. \end{array}$$

2. for the tag size of 64 bits, the constants are

$$\begin{array}{l} d_0 = 1100101 \\ d_1 = 1000011 \\ d_2 = 1111011 \\ d_3 = 0101010 \\ d_4 = 0010001 \\ d_5 = 0000101 \\ d_6 = 1010001 \\ d_7 = 1000010 \\ d_8 = 0011010 \\ d_9 = 0110001 \\ d_{10} = 0011000 \\ d_{11} = 1100110 \\ d_{12} = 0010100 \\ d_{13} = 0101110 \\ d_{14} = 0000001 \\ d_{15} = 1011100. \end{array}$$

3. for the tag size of 128 bits, the constants are

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d_0 = 1100101
d_1 = 1000011
d_2 = 1111010
d_3 = 0101010
d_4 = 0010001
d_5 = 0000101
d_6 = 1010001
d_7 = 1000010
d_8 = 0011010
d_9 = 0110001
d_{10} = 0011000
d_{11} = 1100110
d_{12} = 0010100
d_{13} = 0101110
d_{14} = 0000001
d_{15} = 1011100.
```

The test vectors of the ZUC-256 stream cipher for the keystream generation phase are as follows.

- 1. let $K_i = 0x00$ for $0 \le i \le 31$ and $IV_i = 0x00$ for $0 \le i \le 15$, then the first 20 keystream words are
 - e457e206,cee79e16,7da20fd0,3bbb22cc,a2ec34f0,
 - e4e12c0b,0ad0fb23,6051348a,f9779552,454c3dbb,
 - 397d19b3,28390332,11b9ae54,6094770b,5016e134,
 - 620ebf4a,302c9be3,b65db142,2b564caa,9caeca83
- 2. let $K_i = 0 \text{xff}$ for $0 \le i \le 31$ and $IV_i = 0 \text{xff}$ for $0 \le i \le 15$, then the first 20 keystream words are
 - 7f860542,9c82e263,4ad9a83a,e7d711f6,4eba1791,
 - dfa21089,78d9af94,124a3eee,31feb686,be91bfd5,
 - 148b5e71,9ce309ec,21238b2d,ec2acee4,df347052,
 - 2c5ac5c3,3dc68a27,05c09c6f,2396a67b,091ca2e0

The test vectors of the ZUC-256 stream cipher for the tag authentication phase are as follows.

1. let $K_i = 0x00$ for $0 \le i \le 31$ and $IV_i = 0x00$ for $0 \le i \le 15$, $M = 0x \underbrace{00, \cdots, 00}_{100}$ with the length l = 400-bit, then the 32-bit tag, 64-bit tag and

128-bit tag are

- The 32-bit tag is eb44844f

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- The 64-bit tag is 1018c7fa 1699c153
- The 128-bit tag is 522464ef 930b1b06 a9c6f6bb f22f8cb2
- 2. let $K_i = 0x00$ for $0 \le i \le 31$ and $IV_i = 0x00$ for $0 \le i \le 15$, $M = 0x\underbrace{11, \dots, 11}_{1000}$ with the length l = 4000-bit, then the 32-bit tag, 64-bit tag

and 128-bit tag are

8

- The 32-bit tag is ce1cfddb
- The 64-bit tag is 1007d183 d7780626
- The 128-bit tag is 28991852 93e57bfd f8826b3d 4818749f
- 3. let $K_i = 0$ xff for $0 \le i \le 31$ and $IV_i = 0$ xff for $0 \le i \le 15$, $M = 0x \underbrace{00, \cdots, 00}_{100}$ with the length l = 400-bit, then the 32-bit tag, 64-bit tag and

- The 32-bit tag is **459d34b6**
- The 64-bit tag is 89269bdd 82f4c54a
- The 128-bit tag is fc686d96 081fd6fd dd1c3794 1f9602b0
- 4. let $K_i = 0 \text{xff}$ for $0 \le i \le 31$ and $IV_i = 0 \text{xff}$ for $0 \le i \le 15$, $M = 0x \underbrace{11, \cdots, 11}_{1000}$ with the length l = 4000-bit, then the 32-bit tag, 64-bit tag

and 128-bit tag are

- The 32-bit tag is 5519a0b9
- The 64-bit tag is 3c47d5e3 18508f9d
- The 128-bit tag is 2de05cf5 ad74f35d d114616a 67683bca

The security claim of the ZUC-256 stream cipher with the new initialization scheme is the 256-bit security in the 5G application setting. For the forgery attacks on the authentication part, the security level is the same as the tag size and the IV is not allowed to be re-used. If the tag verification failed, no output should be generated.

3 The Analysis

In this section, we will present the cryptanalysis of the new initialization scheme of ZUC-256 stream cipher, other aspects of the security analysis that is not effected by the change of the IV size and the loading scheme will remain the same as before, and will not cover here.

3.1 Slide Attack

The sliding properties of stream ciphers are used to find sets of related keys where it was shown that a stream cipher may be slidable, in the sense that there exist key-IV values such that the inner state of the cipher at some time t > 0 corresponds to another key-IV loading value. Such key-IV pairs produce the identical keystreams up to a shift by some number of positions and represent related keys [2]. For the loading scheme shown above, it is impossible to find key-IV pairs such that after iterating the cipher for less than 16 initialization steps, the inner state represents a starting inner state for some other key-IV loading value. The fact is due to the choice of the constants in the key/IV loading procedure. In fact, if the values of S_i and S_j (j > i) are different in some positions, it will imply that the inner state after iterating the cipher for j - i steps is not a reasonable starting state. The number of iterating steps, the number of different word states and the detailed indexes are shown in Table 1. Therefore, it is difficult to find related keys to generate the sliding keystreams for ZUC-256 with the new key/IV loading scheme, and even to distinguish the produced keystream of ZUC-256 from random based on the sliding property.

Iterating steps	Number of different states	Indexes of states
1	15	0-14
2	14	0-13
3	13	0-12
4	12	0-11
5	11	0-10
6	10	0-9
7	9	0-8
8	8	0-7
9	7	0-6
10	6	0-5
11	5	0-4
12	4	0-3
13	3	0-2
14	2	0-1
15	1	0

Table 1. Sliding property of ZUC-256 with the new loading scheme

3.2 Differential Attacks

Chosen IV/Key attacks aim at the initialization stage of a stream cipher. For a good stream cipher, after the initialization, each bit of the IV/Key should contribute to each bit of the internal states, and any difference in the IV/Key will result in an almost-uniform and unpredictable difference in the internal states. In stream cipher domain, it is more frequent to change the IV than to change the key. And since the IV is known to the public, so the chosen-IV attack is more feasible. The main idea of chosen-IV attack is to choose some differences in some IV bits and study the propagation of the differences during the initialization of the cipher.

To evaluate the diffusion of the input difference in IV effectively, we make the following two assumptions:

- 10 ZUC Design Team Chinese Academy of sciences
- 1. If the input difference to the FSM is not zero, then the output difference of FSM is all 1. As L is an MDS matrix and S is non-linear permutation, the difference is diffused sufficiently and faster than the LFSR.
- 2. The modular addition operation is reduced to be the traditional xor. The diffusion of difference in modular addition is related to the values of states. Meanwhile, the modular addition can be seen as the xor with carry. Thus, it is reasonable to follow this assumption to a certain extent.

In order to evaluate the property of initialization stage comprehensively, we give three kinds of analysis.

Firstly, we want to know the minimum number of iteration steps to guarantee that each bit of feedback is influenced by each bit in the initialization state. We divide the initialization state into $16 \times 31 = 496$ bits and test the least number of rounds that each bit is inserted into FSM. The obtained results are shown in Table 2, where 'Location' denotes the index *i* of s_i and the leftmost location is denoted by 15. Combining with the key/IV loading procedure, we can conclude that the difference of IV is diffused to FSM after at most four rounds and the memory cells are influenced after at most five rounds.

Table 2. Least number of rounds that every bit is inserted into FSM

Location	Diffusion rounds
0	$6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6$
1	777777788888887777777777777777777777
2	888888899999998888888888888888888888888
3	9 9 9 9 9 9 9 9 9 10 10 10 10 10 10 10 9 9 9 9
4	$7\ 7\ 7\ 7\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\ 7\$
5	11111111111111117777
6	$2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2$
7	$3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\$
8	$4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4$
9	$1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\$
10	$2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2\ 2$
11	$3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 3\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\$
12	$4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4\ 4$
13	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 3
14	$6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6$
15	$6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 6\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\ 5\$

The conclusion mentioned above is tested under two assumptions and may be different to the real results. We randomly choose 2^{11} (K, IV) pairs to test the diffusion property in practice. In details, just exhaustively test all the possible differences for *i*-th ($0 \le i \le 15$) word of IV to get the maximum iteration steps for causing difference in memory cells R_1 and R_2 . The results of experiments are summarized as Table 3.

i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R_1	1	2	3	4	2	3	4	5	1	2	3	4	2	3	4	5
R_2	2	3	4	5	1	2	3	4	2	3	4	5	1	2	3	4

Table 3. Maximum steps to lead difference in R_1 and R_2

We can see that the memory cells are influenced after at most five rounds from Table 3 and the result matches the above conclusion from Table 2.

Secondly, the minimum number of iterations to guarantee that each bit of the register state is influenced by each bit of initialization state will be focused. In a word, if the input to FSM is different, then the state of the feedback word s_{15} will have some difference in the next round. The differential state will be shifted to the rightmost location in the next 15 rounds and all the states will be affected.

We have also made some experiments to evaluate this diffusion property in practice. For the injected difference position on each bit of IV, we have chosen 2^{22} (K, IV) pairs to get the least number of steps that all the register states are influenced. The experimental results show that each bit of register state is affected by each bit of IV after at most 19 rounds.

Thirdly, we will investigate the differential characteristic aspect of the initialization scheme when the injected difference positions covering all the possible key and IV loading positions.

We have searched the minimum number of active s-box of the initialization scheme under the simplification that the $2^{31} - 1$ addition operation of the LFSR be replaced by the traditional exclusive or. The searching result shows that there are some input key differences such that the minimum number of active s-box is zero after 11 rounds of initialization, when the hamming weight of the input difference is restricted to be less than 11. The following are the only 43 input difference patterns, shown in Table 4. Given that s_2 and s_6 are chosen to have the non-zero input difference B and A, where A is located in the least significant 16 bit of s_6 , we list the difference propagation process in the Table 5. We have experimentally checked all the 43 input difference patterns to see the precise differential propagation process and tried to detect if there is some bias existing in each of the 31 bits of s_0 for 33 initialization rounds. In all the cases, there is no bias detected in our search. We have also found that the difference will propagate slowly if the difference is cancelled to be zero in s_{15} after 3 rounds. Table 5 gives the difference propagation of the 16 cells of the LFSR after i rounds of iteration $(i = 1, 2, \dots, 27)$ in a step-by-step manner. It is easy to see that the memory cells R_1 and R_2 have no difference even after 11 rounds, thus the differences C-H are generated only from the $2^{31} - 1$ addition operation. We expect that the state cells s_{15} and s_{14} will have good differential randomness after 32 rounds. Hence, we believe that, after 33 rounds of iteration, the difference in the first 32-bit keystream word will be fairly random and unpredictable. Note that the above analysis will naturally be converted into a related key attack scenario, which is

Index K_2 K_{18} K_{26} K_{22} K_{30} Index K_2 K_{18} K_{26} K_{22} K_{30} 0x81 | 0x80 | 0x80 | 0x0c | 0x000x88 | 0x80 | 0x80 | 0x44 | 0x480220x02 0x00 0x00 0x10 0x10 230x30 0x30 0x30 0x01 0x83 1 $\mathbf{2}$ 0x01 0x00 0x00 0x08 0x08 240x11 0x10 0x10 0x08 0x89 3 0x04 0x00 0x00 0x20 0x20 250x06 0x00 0x00 0x30 0x30 4 0x42 0x40 0x40 0x12 0x14 260x07 0x00 0x00 0x38 0x3850x08 0x00 0x00 0x40 0x40 270xc0 0xc0 0xc0 0x06 0x0c6 0x21 0x20 0x20 0x09 0x0a $\overline{28}$ 0x0b 0x00 0x00 0x58 0x587 0x41 0x40 0x40 0x0a 0x0c $\overline{29}$ 0xa0 0xa0 0xa0 0x05 0x0a 8 0x83 0x80 0x80 0x1c 0x10 30 0x28 0x20 0x20 0x41 0x42 9 0x85 0x80 0x80 0x2c 0x2031 0x0a 0x00 0x00 0x50 0x50 0x14 0x10 0x10 0x20 0xa1 10 320x82 0x80 0x80 0x14 0x18 0x24 0x20 0x20 0x21 0x22 11 0x09 0x00 0x00 0x48 0x48 33 120x10 0x10 0x10 0x00 0x81 34 0x0d 0x00 0x00 0x68 0x68 13 0x20 0x20 0x20 0x01 0x02 35 0x84 0x80 0x80 0x24 0x28 14 0x18 0x10 0x10 0x40 0xc1 36 0x48 0x40 0x40 0x42 0x44 150x89 0x80 0x80 0x4c 0x40 37 0x0c 0x00 0x00 0x60 0x60 0x03 0x00 0x00 0x18 0x18 0x12 0x10 0x10 0x10 0x91 38 160x22 0x20 0x20 0x11 0x12 0x0e 0x00 0x00 0x70 0x70 39 170x90 0x90 0x90 0x04 0x89 0x05 | 0x00 | 0x00 | 0x28 | 0x2840 180x80 0x80 0x80 0x04 0x08 19410x60 | 0x60 | 0x60 | 0x03 | 0x0620 0x40 0x40 0x40 0x02 0x04 42 0x50 0x50 0x50 0x02 0x85210x44 0x40 0x40 0x22 0x24

Table 4. The differences of the LFSR in each round of iteration

13

Round	S_{15}	S_{14}	S_{13}	S_{12}	S_{11}	S_{10}	S_9	S_8	S_7	S_6	S_5	S_4	S_3	S_2	S_1	S_0	R_1	R_2
0	0	0	0	0	0	0	0	0	0	Α	0	0	0	В	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	Α	0	0	0	В	0	0	0
2	0	0	0	0	0	0	0	0	0	0	0	А	0	0	0	В	0	0
3	0	0	0	0	0	0	0	0	0	0	0	0	А	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0	0	0	0	Α	0	0	0	0
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	А	0	0	0
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	Α	0	0
7	С	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
8	D	С	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
9	Е	D	С	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	F	Е	D	С	0	0	0	0	0	0	0	0	0	0	0	0	0	0
11	G	F	Е	D	С	0	0	0	0	0	0	0	0	0	0	0	0	0
12	Η	G	F	Е	D	С	0	0	0	0	0	0	0	0	0	0	0	*
13	*	Η	G	F	Е	D	С	0	0	0	0	0	0	0	0	0	*	*
14	*	*	Η	G	F	Е	D	C	0	0	0	0	0	0	0	0	*	*
15	*	*	*	Η	G	F	Е	D	С	0	0	0	0	0	0	0	*	*
16	*	*	*	*	Η	G	F	Е	D	С	0	0	0	0	0	0	*	*
17	*	*	*	*	*	Η	G	F	Е	D	C	0	0	0	0	0	*	*
18	*	*	*	*	*	*	Η	G	F	Е	D	С	0	0	0	0	*	*
19	*	*	*	*	*	*	*	Η	G	F	E	D	С	0	0	0	*	*
20	*	*	*	*	*	*	*	*	Η	G	F	Е	D	С	0	0	*	*
21	*	*	*	*	*	*	*	*	*	Η	G	F	Е	D	С	0	*	*
22	*	*	*	*	*	*	*	*	*	*	Η	G	F	Е	D	C	*	*
23	*	*	*	*	*	*	*	*	*	*	*	Η	G	F	Е	D	*	*
24	*	*	*	*	*	*	*	*	*	*	*	*	Η	G	F	E	*	*
25	*	*	*	*	*	*	*	*	*	*	*	*	*	Η	G	F	*	*
26	*	*	*	*	*	*	*	*	*	*	*	*	*	*	Η	G	*	*
27	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	Η	*	*

Table 5. The differences of the LFSR in each round of iteration

14 ZUC Design Team Chinese Academy of sciences

difficult, in stream cipher domain, to detect the related key pairs given only the corresponding keystream segments.

From the above analysis, we could conclude that the new initialization scheme of ZUC-256 could provide the 256-bit security in 5G application settings.

4 Conclusions

In this paper, we have presented the details of a new initialization scheme for the ZUC-256 stream cipher that works with the 128-bit initialization vector. Any cryptanalysis of both the original and the new initialization scheme is welcome.

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